# Knowledge Rich Curriculum Plan 

Year 12 Maths
Unit 13 - Integration

| Maths Year 12 | Unit: Integration |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Lesson/Learning Sequence | Intended Knowledge: <br> Students will know that. | Tiered Vocabulary | Prior Knowledge: <br> In order to know this students, need to already know that. | Assessment |
| Lesson 69: <br> Integrating/Indefinite integrals <br> Lesson Objective: To learn how to integrate expressions. | - Students will know that integration is the reverse process of differentiation. <br> - Students will know to integrate by adding one to the power and then dividing by the new power. <br> - Students will know how to integrate a constant. <br> - Students will know how to integrate expressions with coefficients. <br> - Students will know how to integrate multiple terms by integrating each term separately. <br> - Students will know that integration can only be done when a term is simplified to a single power of $x$. <br> - Students will know to add in the constant of integrating whenever an integration takes place unless given limits. <br> - Students will understand integration notation. |  | - Students need to know how to manipulate algebraic terms using index laws. <br> - Students need to know how to differentiate expressions. <br> - Students need to know that when you differentiate constants they disappear. <br> - Students need to know how to expand brackets. |  |
| Lesson 70: Finding functions Lesson Objective: To learn how to how to find the constant of integration. | - Students will know how to find the constant of integration when given any point that the curve passes through. <br> - Students will know to integrate the function, substitute the $x$ - and $y$-coordinates and solve to find $c$. |  | - Students need to know how to integrate functions with multiple terms. <br> - Students need to know why the constant of integration is used. <br> - Students need to know how to use substitution. <br> - Students need to know how to rearrange formulae. <br> - Students need to know how to solve equations. <br> - Students need to know how to differentiate expressions. <br> - Students need to know how to use index laws to simplify expressions. <br> - Students need to know to only integrate when each term is being expressed as a single power of $x$. <br> - Students need to know how to collect like terms. |  |
| Lesson 71: Definite integrals Lesson Objective: To learn how to find a definite integral. | - Students will know that a definite integral is when you calculate an integral between two limits. <br> - Students will know that a definite integral usually produces a value whereas an indefinite integral always produces a function. <br> - Students will know how to use the correct notation for each stage of the process. |  | - Students need to know how to integrate functions with multiple terms. <br> - Students need to know how to use index laws to simplify expressions. <br> - Students need to know that integration can only happen when each of the terms are written as a single power of $x$. <br> - Students need to know how to use substitution. |  |


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|  | - Students will know how to write a statement of integration with limits. <br> - Students will know that the constant of integration is not needed when limits are known. <br> - Students will know to integrate, then substitute in the limits and find the difference between the answers. <br> - Students will know that all solutions to indefinite integrals are positive because it represents an area. |  | - Students need to know how to use the order of operations. |  |
| Lesson 72: Areas under curves <br> Lesson Objective: To learn how to find the area under a curve. | - Students will know that definite integration can be used to find the area under a curve. <br> - Students will know how to use the definite integral to find the area under a curve by integrating the function, substituting in the limits and finding the difference between them. <br> - Students will know that areas below the curve but above the x -axis are always positive. <br> - Students will know how to identify the area to find by sketching the graph and using the limits. |  | - Students need to know how to integrate functions with multiple terms. <br> - Students need to know how to find definite integrals. <br> - Students need to know that a constant of integration is not needed when limits are known. <br> - Students need to know how to use substitution. <br> - Students need to know how to sketch quadratic and cubic graphs. <br> - Students need to know that areas are positive. <br> - Students need to know how to factorise expressions. <br> - Students need to know how to solve quadratic and cubic equations. |  |
| Lesson 73: Areas under the $x$-axis Lesson Objective: To learn how to find the area bounded by a curve and is below the $x$-axis. | - Students will know that an area below the $x$-axis will produce a negative answer. <br> - Students will know to change the negative answer to a positive solution of the area. <br> - Students will know how to find the area total area when parts of the area are above the $x$-axis and part of the area are below the $x$-axis. <br> - Students will know that all area solutions should be positive. |  | - Students need to know how to find the area under a curve. <br> - Students need to know how to find the area bounded by a curve above the $x$-axis. <br> - Students need to know how to integrate functions with multiple terms. <br> - Students need to know how to sketch cubic graphs. <br> - Students need to know how to factorise expressions. <br> - Students need to know how to solve quadratic and cubic equations. <br> - Students need to know how to use substitution. <br> - Students need to know how to find compound areas. |  |


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|  |  |  | - Students need to know how to find the definite integral using limits. |  |
| Lesson 74: Areas between curves and lines Lesson Objective: To learn how to find the area bounded by curves and lines. | - Students will know how to use definite integration together with areas of trapeziums and triangles to find more complicated areas on graphs. <br> - Students will know how to identify possible shapes and areas on graphs to find the area needed. |  | - Students need to know how to integrate functions with multiple terms. <br> - Students need to know how to use substitution. <br> - Students need to know how to use simultaneous equations to find the points of intersection. <br> - Students need to know how to find the area under a curve. <br> - Students need to know how to find the area bounded by a curve above the $x$-axis. <br> - Students need to know how to find the area bounded by a curve below the x-axis. <br> - Students need to know how to find the total area when parts of the area are above the $x$-axis and part of the area is below the $x$-axis. <br> - Students need to know how to sketch quadratic and cubic graphs. <br> - Students need to know how to solve quadratic and cubic equations. <br> - Students need to know how to factorise expressions. <br> - Students need to know how to find the areas of rectangles, triangles and trapeziums. <br> - Students need to know how to find compound areas. |  |

